# Modelling multiple fish quota markets with discarding

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- Species/stock-specific quotas

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$$H = H(E)$$
  

$$h_i = \beta_i H, \quad i = 1, 2, ..., M$$
  

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 Given quota (lease) prices r<sub>i</sub>, the profit maximising harvest H<sup>\*</sup> satisfies

$$\sum_{i}\beta_{i}\left[p_{i}-r_{i}\right]-c=\lambda\geq0$$

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• Discards are  $h_i - q_i(r_i) \ge 0$ 

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▶ For a representative vessel, H<sup>\*</sup> satisfies

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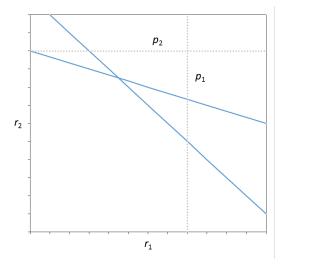
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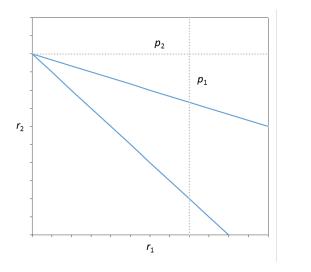
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- With r<sub>1</sub> = p<sub>1</sub>, vessels are *indifferent* between discarding and landing Species 1
- Individual demands for Species 1 quota are indeterminate

$$eta_1\left[ p_1 - r_1 
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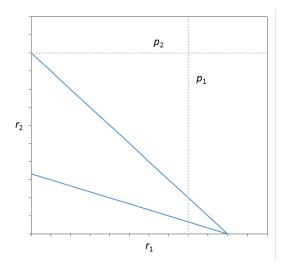
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Species 1 quota valued at the entire marginal value of harvest

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- Quota prices determined out of equilibrium (heuristic)?

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- Determine maximal (uniform, linear) quota prices...

# Scenario 1

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## Scenario 2

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62 63		0.40	0.30			h2		505.00	707.00	707.00	1919.00																
03 01		10.00	10.0			h3		808.00	505.00	606.00	1919.00	TAC	rmax			10 -											
2		8.00	8.00			q1		707.00	808.00	707.00	2222.00		0.00	10.00													
3		7.00	7.00			41 92		505.00	358.00	707.00	1600.00		8.00	8.00													
1		0.00		7.00		q3		808.00	505.00	606.00	1919.00		0.00	7.00		5 -				_							
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3		0.00				12		505.00	358.00	707.00	1600.00					4 -				_							
		4104				ñ		808.00	505.00	606.00	1919.00		r min	d max													
						d1		0.00	0.00	0.00	0.00		0.00	10000													
	2200					d2		0.00	319.00	0.00	319.00		8.00	10000		0 -											
	1900					d3		0.00	0.00	0.00	0.00		0.00	10000				1			2		3				
	1900					v1		7070.00	8080.00	7070.00																	
						¥2		4040.00	3104.00	5656.00										Harua	st/Quot	19					
	2300					¥3		5656.00	3535.00	4242.00		total								marve	ny quoi						
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						r3q3		0.00	0.00	0.00																	
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## Scenario 3

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c		1.75	1.90	1	L.95		н		2020.00	2020.00	1108.57	2020.00		-						Quet	a Price,	EV D	ice				
b		0.35	0.40	0	0.35		C(H)		3535.00	3838.00	2161.71				LO?	YES	• 12 -			Cau	a r neeg		100				
ь	2	0.25	0.35		0.35		h1		707.00	808.00	388.00	1903.00	_														
ь	3	0.40	0.25		0.30		h2		505.00	707.00	388.00	1600.00					10 -										
p		10.00	10.0	1	0.00		h3		808.00	505.00	332.57	1645.57	TAC	r max													
p	2	8.00	8.00		3.00		q1		707.00	808.00	388.00	1903.00	2300	0.00	100.00		- a -										
p		7.00	7.00		7.00		q2		505.00	707.00	388.00	1600.00	1600	100.00	100.00												
r		0.00					q3		808.00	505.00	332.57	1645.57	2500	0.00	100.00		0										
12		18.43					n.		707.00	808.00	388.00	1903.00					4 -				_						
r3		0.00					12		505.00	707.00	388.00	1600.00															
							8		808.00	505.00	332.57	1645.57		r min	d max		2										
							d1		0.00	0.00	0.00	0.00		0.00	0												
	2200						d2 d3		0.00	0.00	0.00	0.00		0.00	0		0		1		2			3			
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	2300						¥2 ¥3		5656.00		2328.00		total							Ha	arvest/0	Juota					
	1600						profit			13433.00			33814.29				3000										
	2500						prom			19433.00	140040		33004.23				2500										
ŀ	2.000						rtot		0.00	0.00	0.00						2500										
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Modelling work in progress...

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